

## Worked Solutions

Pure Maths, Differential Calculus,

sheet PM-DIFF-PR-01

### The Product Rule Q.10

differentiate the function  $y = \sin(3x)\cos(2x)$

The **Product Rule** states that if  $y = u(x) \cdot v(x)$

then:

$$\frac{dy}{dx} = \frac{du}{dx} \cdot v(x) + u(x) \cdot \frac{dv}{dx}$$

let  $u(x) = \sin(3x)$  then  $\frac{du}{dx} = 3\cos(3x)$

let  $v(x) = \cos(2x)$  then  $\frac{dv}{dx} = -2\sin(2x)$

substituting into the Product Rule equation:

$$\frac{dy}{dx} = 3\cos(3x) \cdot \cos(2x) + \sin(3x) \cdot (-2\sin(2x))$$

simplifying,

$$\frac{dy}{dx} = 3\cos(3x)\cos(2x) - 2\sin(3x)\sin(2x)$$

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